Mass of Xenon in Vessel at Maximum Operating Pressure (absolute):

We presently have a total of 100 kg Xe. if we do not obtain more then our maximum operating pressure (assuming we have negligible volume in gas purification system, including recovery vessel) is then computed as follows:

Pressure vessel has internal dimensions length, radius:

$$L_{pv} := 2.1m$$
 $R_{i pv} := 57cm$

Total Vessel internal volume is:

 $v_{ves} \coloneqq 2.001 \text{m}^3 \quad \text{from CAD measurement (no nozzle vol; assume all but one nozzle are mostly filled; we will add 2 nozzle vols to main vol)}$

$$V_{\text{noz}} := \pi 5 \text{cm}^2 \cdot 32 \text{cm}$$
 $V_{\text{noz}} = 5.027 \times 10^{-4} \text{m}^3$

Internal component volume sum

PMT enclosures (cans)

$$r_{o can} := 4.4cm$$
 $l_{can} := 16cm$

$$v_{can} := \pi r_{o_can}^2 \cdot l_{can}$$
 $v_{can} = 9.731 \times 10^{-4} \text{ m}^3$

$$v_{cans} := 60v_{can}$$
 $v_{cans} = 0.058 \,\mathrm{m}^3$

PMT mounting plate

$$v_{mn} \coloneqq .0104m^3$$
 from CAD measurement

SiPM electronics shield

$$v_{\rm sh} := .086 {\rm m}^3$$
 from CAD measurement

Assume field cage, mesh frames and SiPM boards are negligible

Net internal volume:

$$V_{int} := (V_{ves} + 2V_{noz}) - (v_{cans} + v_{mp} + v_{sh})$$
 $V_{int} = 1.847 \,\text{m}^3$

Total amount of xenon

$$M_{Xe_100} = 100 \text{kg}$$

Operating Temperature, physical constants:

$$T_{amb} := 293K R := 8.314J \cdot mol^{-1} \cdot K^{-1} \qquad M_{a_Xe} := 136gm \cdot mol^{-1}$$

Critical Pressure, temperature of Xenon:

$$P_{c_Xe} := 58.40 \text{bar}$$
 $T_{c_Xe} := 15.6 \text{K} + 273 \text{K}$ $T_{c_Xe} = 288.6 \text{ K}$

reduced pressure:

$$P_{r_8bar} := \frac{9bar}{P_{c_Xe}} \qquad P_{r_8bar} = 0.154$$

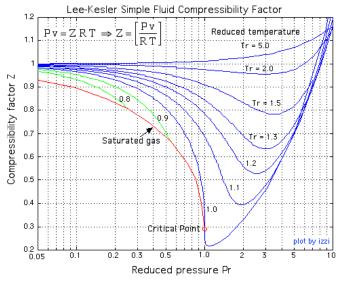
reduced temperature

$$T_r := \frac{T_{amb}}{T_{c Xe}} \qquad T_r = 1.015$$

Compressibility Factor:

from chart for pure gasses shown below

$$Z_{Xe\ 9bar} := .94$$



ref: A Generalized
Thermodynamic Correlation
based on Three-Parameter
Corresponding States, B.I.Lee &
M.G.Kesler, AlChE Journal,
Volume 21, Issue 3, 1975, pp.
510-527' (secondary ref.
from:http://www.ent.ohiou.edu/~-thermo/

Fig. 6 Compressibility Factor, pure gasses

Number of moles:

$$n_{\text{Xe_100}} := \frac{M_{\text{Xe_100}}}{M_{\text{a Xe}}}$$
 $n_{\text{Xe_100}} = 735.294 \,\text{mol}$

Operating pressure is:

$$P_{100kg_tot} := \frac{{}^{n}Xe_100 \cdot {}^{z}Xe_9bar \cdot {}^{R} \cdot {}^{T}amb}{V_{int}} \qquad P_{100kg_tot} = 9.1 \, bar$$

Density is:

$$\rho_{100kg_tot} \coloneqq \frac{^{n}\text{Xe_100} \cdot M_{a_Xe}}{V_{int}} \qquad \qquad \rho_{100kg_tot} = 0.054 \frac{gm}{cm^3}$$

Mass of xenon in active volume

$$l_{av} := 1.3m$$
 $r_{av} := 53cm$ $V_{av} := \pi r_{av}^2 \cdot l_{av}$ $V_{av} = 1.147 \,\text{m}^3$ $M_{av} := M_{Xe_100} \cdot \frac{V_{av}}{V_{int}}$ $M_{av} = 62.1 \,\text{kg}$